WORKSHEET 9/11/23 MATH 2331, FALL 2023

(1) Consider the following system of equations:

$$2x + 4y - 2z = -10$$

$$3x + 6y = -12$$

$$y + z = 3$$

- (a) What is the coefficient matrix A of the system?
- (b) What is the augmented matrix of the system?
- (c) Use Gauss–Jordan elimination to solve the system.
- (d) What is the reduced row echelon form of A (notation: rref(A))?
- (2) Given the reduced row-echelon form of the matrix, how many solutions does the corresponding system of linear equations have?
 - (a)

(a)	$\begin{bmatrix} 1 & 0 & 0 & & 4 \\ 0 & 1 & 0 & & 3 \\ 0 & 0 & 1 & & 1 \\ 0 & 0 & 0 & & 0 \end{bmatrix}$
(b) (c)	$\begin{bmatrix} 1 & 0 & 0 & & 4 \\ 0 & 1 & 7 & & 3 \end{bmatrix}$
(d)	$\begin{bmatrix} 0 & 1 & 0 & & 1 \\ 0 & 0 & 0 & & 0 \\ 0 & 0 & 0 & & 0 \\ 0 & 0 & 0 & & 0 \\ 0 & 0 & 0 & & 0 \end{bmatrix}$
	$\begin{bmatrix} 1 & 0 & 0 & & 0 \\ 0 & 1 & 0 & & 0 \\ 0 & 0 & 1 & & 0 \\ 0 & 0 & 0 & & 1 \end{bmatrix}$
(e)	$\begin{bmatrix} 1 & 2 & 3 & & 4 \end{bmatrix}$

(f)	
~ /	$\begin{bmatrix} 1 & 0 & & 1 \\ 0 & 1 & & 2 \\ 0 & 0 & & 1 \\ 0 & 0 & & 0 \\ 0 & 0 & & 0 \end{bmatrix}$
	$0 \ 1 \ \ 2$
	$0 \ 0 \ \ 1$
(g)	F . A
	$\begin{bmatrix} 1 & & 1 \\ 0 & & 2 \\ 0 & & 7 \end{bmatrix}$

(3) For which values of k is the system of linear equations

$$2x + 2y + kz = 3$$
$$kx + ky + 8z = k + 2$$

consistent? When it is consistent, for which values is there a unique solution, and for which values are there infinitely many?