## WORKSHEET 10/12/23 <br> MATH 2331, FALL 2023

(1) Suppose that $\mathfrak{B}=\left\{\vec{v}_{1}, \vec{v}_{2}, \vec{v}_{3}\right\}$ is a basis for $\mathbb{R}^{3}$. What is $\left[\vec{v}_{2}\right]_{\mathfrak{B}}$ ?
(2) Suppose that $A=S^{-1} B S$. Are $A$ and $B$ similar?
(3) Suppose that $T$ is a linear transformation with matrix $A$, and that $A=S B S^{-1}$. In which basis does $B$ represent $T$ ?
(4) Describe the columns of $[T]_{\mathfrak{B}}$.
(5) Is there a basis for $\mathbb{R}^{2}$ in which reflection over the line $L$ is represented by a diagonal matrix?
(6) Is there a basis for $\mathbb{R}^{2}$ in which a 90 degree rotation is represented by a diagonal matrix?

