WORKSHEET 10/16/23 MATH 2331, FALL 2023

In these problems, $\vec{u}_1 = \frac{1}{2}(1, 1, 1, 1)$, $\vec{u}_2 = \frac{1}{2}(1, 1, -1, -1)$, $\vec{u}_3 = \frac{1}{2}(1, -1, 1, -1)$, and $V = \text{Span}(\vec{u}_1, \vec{u}_2, \vec{u}_3)$.

- (1) Can you find a vector \vec{u}_4 such that $\vec{u}_1, \ldots, \vec{u}_4$ are orthonormal?
- (2) Suppose that $c_1\vec{u}_1 + c_2\vec{u}_2 + c_3\vec{u}_3 = \vec{0}$. What can you say about c_1 , c_2 , and c_3 ? If you're writing down a matrix, you're working too hard!
- (3) Find a basis for V. Don't work too hard!
- (4) Extend your basis from #3 to a basis \mathfrak{B} for \mathbb{R}^4 . Don't work too hard!
- (5) Given a vector \vec{x} in \mathbb{R}^4 , what is $[\vec{x}]_{\mathfrak{B}}$? If you're writing down a matrix, you're working too hard!

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